## Metric-Affine Effective Field Theory, Inflation and Reheating

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Mainly based on
G. Pradisi, A S., EPJC, 2206.15041

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\text { A.S., PRD, } 2207.08830
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## Introduction

- Einstein's general relativity (GR) explains gravity in geometrical terms:
- distances are measured through the metric $g_{\mu \nu}$
- the gravitational force is determined by the (affine) Levi-Civita connection $\Gamma_{\mu}{ }^{\rho}{ }_{\sigma}$

This beautiful construction (which flows from the equivalence principle) accounts for all gravitational observations performed so far, including today's nearly-exponential accelerated expansion of the universe if the cosmological constant is present.

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This beautiful construction (which flows from the equivalence principle) accounts for all gravitational observations performed so far, including today's nearly-exponential accelerated expansion of the universe if the cosmological constant is present.

From the purely geometrical point of view $g_{\mu \nu}$ and $\mathcal{A}_{\mu}{ }^{\rho}{ }_{\sigma}$, unlike in GR, can be completely independent objects and, moreover, can contain extra degrees of freedom besides the spin-2 graviton. This generalized scenario is known as metric-affine gravity.

## Necessary ingredients for gravitational theories

To implement the general relativity principle, which states that all laws of physics should be invariant under general coordinate transformations, we need

- the metric $g_{\mu \nu}$ to define distances
- the connection $\mathcal{A}_{\mu}{ }^{\rho}{ }_{\sigma}$ to define covariant derivatives

$$
\rightarrow \text { distorsion } \equiv C_{\mu}{ }^{\rho}{ }_{\sigma} \equiv \mathcal{A}_{\mu}{ }^{\rho}{ }_{\sigma}-\Gamma_{\mu}{ }^{\rho}{ }_{\sigma}, \quad \text { (a tensor) }
$$

The curvature associated with $\mathcal{A}_{\mu}{ }^{\rho}{ }_{\sigma}$ is defined by

$$
\begin{aligned}
\mathcal{F}_{\mu \nu}{ }^{\rho}{ }_{\sigma} & \equiv \partial_{\mu} \mathcal{A}_{\nu}{ }^{\rho}{ }_{\sigma}-\partial_{\nu} \mathcal{A}_{\mu}{ }^{\rho} \sigma_{\sigma}+\mathcal{A}_{\mu}{ }^{\rho}{ }_{\lambda} \mathcal{A}_{\nu}{ }^{\lambda} \sigma^{\prime}-\mathcal{A}_{\nu}{ }^{\rho}{ }_{\lambda} \mathcal{A}_{\mu}{ }^{\lambda} \sigma^{\prime} \\
& =R_{\mu \nu}{ }^{\rho}{ }_{\sigma}+D_{\mu} C_{\nu}{ }^{\rho}{ }_{\sigma}-D_{\nu} C_{\mu}{ }^{\rho}{ }_{\sigma}+C_{\mu}{ }^{\rho}{ }_{\lambda} C_{\nu}{ }^{\lambda}{ }_{\sigma}-C_{\nu}{ }^{\rho}{ }_{\lambda} C_{\mu}{ }^{\lambda}{ }_{\sigma},
\end{aligned}
$$

where $R_{\mu \nu}{ }^{\rho}{ }_{\sigma}$ is the standard Riemann tensor and $D_{\mu}$ is the covariant derivative computed with the Levi-Civita connection. We can define a scalar

$$
\mathcal{R} \equiv \mathcal{F}_{\mu \nu}{ }^{\mu \nu}
$$

and a pseudoscalar [Hojman, Mukku, Sayed (1980); Nelson (1980); Holst (1995)]

$$
\text { "Holst invariant" } \equiv \mathcal{R}^{\prime} \equiv \frac{1}{\sqrt{-g}} \epsilon^{\mu \nu \rho \sigma} \mathcal{F}_{\mu \nu \rho \sigma},
$$

where $\epsilon^{\mu \nu \rho \sigma}$ is the totally antisymmetric Levi-Civita symbol with $\epsilon^{0123}=1$.
$\mathcal{R}^{\prime}=0$ for $C_{\mu}{ }^{\rho}{ }_{\sigma}=0$ as $R_{\mu \nu \rho \sigma}+R_{\nu \sigma \rho \mu}+R_{\sigma \mu \rho \nu}=0$
For a recent overview [Baldazzi, Melichev, Percacci (2021)]

## Adding matter

Consider a generic number of

- real scalars (or pseudoscalars) $\phi$
- gauge (covariant vector) fields $A_{\mu}^{I}$ corresponding to an internal gauge group $G$
- Weyl fermions $\psi$

In the presence of fermions $\mathcal{D}_{\mu} g_{\alpha \beta}=0$ (metric compatibility)
The gauge fields $A_{\mu}^{I}$, together with the connection $\mathcal{A}_{\mu}{ }^{\rho}{ }_{\sigma}$, allow us to define covariant derivatives with respect to both general coordinate transformations and $G$ :

$$
\mathcal{D}_{\mu} \phi=\partial_{\mu} \phi+i \theta^{I} A_{\mu}^{I} \phi, \quad \mathcal{D}_{\mu} \psi=\partial_{\mu} \psi+i t^{I} A_{\mu}^{I} \psi+\frac{1}{2} \mathcal{A}_{\mu}^{a b} \sigma_{a b} \psi,
$$

where $\sigma^{a b} \equiv \frac{1}{4}\left(\sigma^{a} \bar{\sigma}^{b}-\sigma^{b} \bar{\sigma}^{a}\right)$, also $\sigma^{i} \equiv-\bar{\sigma}^{i}(i=1,2,3)$ are the Pauli matrices and $\sigma^{0} \equiv \bar{\sigma}^{0} \equiv 1$ is the $2 \times 2$ identity matrix. The gauge couplings are in the $G$-generators $\theta^{I}$ and $t^{I}$.

Also, we can define the field strength associated with $G$

$$
F_{\mu \nu}^{I} \equiv \partial_{\mu} A_{\nu}^{I}-\partial_{\nu} A_{\mu}^{I}-f^{K J I} A_{\mu}^{K} A_{\nu}^{J}
$$

and the $f^{K J I}$ are the structure constants of $G$. It is always a tensor

## General theories with non-dynamical distorsion

The most general local effective field theory with non-dynamical $C_{\mu}{ }^{\rho}{ }_{\sigma}$ has action

$$
S_{\mathrm{eq}}=\int d^{4} x \sqrt{-g}\left(\mathcal{F}_{\mu \nu \rho \sigma} \mathcal{T}^{\mu \nu \rho \sigma}(\Phi)+\Sigma(\Phi, \mathcal{D} \Phi, C)\right)
$$

where $\Phi$ represents the set of fields that are independent of $C_{\mu}{ }^{\rho}{ }_{\sigma}$, namely

$$
\Phi=\left\{g_{\mu \nu}, \phi, \psi, F_{\mu \nu}^{I}, \ldots\right\},
$$

the dots are curvatures and covariant derivatives of the previous fields constructed with the Levi-Civita connection.

When the action has the form $S_{\text {eq }}$ the distorsion is not dynamical because the field equations of $C_{\mu}{ }^{\rho}{ }_{\sigma}$ are purely algebraic in $C_{\mu}{ }^{\rho}{ }_{\sigma}$. Therefore, in principle, these equations can be solved exactly to find $C_{\mu}{ }_{\mu}{ }_{\sigma}$ as a functional of $\Phi$. Once this is done, the theory with action $S_{\text {eq }}$ can always be written as a metric theory.

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We can thus state that the theories with non-dynamical distorsion are those whose action is linear in the curvature $\mathcal{F}_{\mu \nu}{ }^{\rho}{ }_{\sigma}$ of the full connection $\mathcal{A}_{\mu}{ }^{\rho}{ }_{\sigma}$ with the "coefficients" of the linear terms, i.e. the tensor $\mathcal{T}^{\mu \nu \rho \sigma}(\Phi)$, being independent of the distorsion itself.

## Theories with dynamical distorsion

The general form, $S_{\text {eq }}$, of theories with non-dynamical distorsion is useful, among other things, because it allows us to identify those theories with a dynamical distorsion: they are those whose action can never be brought into the form $S_{\text {eq }}$.

Example

$$
S=\int d^{4} x \sqrt{-g}\left(\mathcal{F}_{\mu \nu \rho \sigma} \mathcal{T}^{\mu \nu \rho \sigma}(\Phi)+\Delta\left(\Phi, \mathcal{R}, \mathcal{R}^{\prime}\right)+\Sigma(\Phi, \mathcal{D} \Phi, C)\right)
$$

barring specific choices of the action (e.g.
$\left.\Delta=\Delta\left(\Phi, \alpha(\Phi) \mathcal{R}+\beta(\Phi) \mathcal{R}^{\prime}\right), \Sigma=\Sigma(\Phi, \mathcal{D} \Phi)\right)$

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$\rightarrow$ Can the inflaton be identified with an extra dynamical component of the connection?

The main motivation for answering this question is to understand whether the inflaton can have a geometrical origin too

## Inflation: introduction

Inflation is a nearly-exponential expansion that occurred during the early stages of the universe.

- It is driven by a spin-0 field, the inflaton
- The inflaton has an appropriate potential, which guarantees that such an expansion not only occurred, but also eventually came to an end: a reheating must take place after inflation in order to generate all particles we observe


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Who is the inflaton? Are the observational bounds satisfied?

To do list

- Find whether the connection contains a spin-0 field with an appropriate potential
- Identify the region of parameter space with viable values of the scalar spectral index $n_{s}$, the tensor-to-scalar ratio $r$ and the curvature power spectrum $P_{R}$ [Planck collaboration (2018); BICEP/Keck collaboration (2021) (BK18)]
- Understand whether an efficient production of known particles, such as electrons, quarks and Higgs bosons (reheating) can take place after inflation


## The key idea

When $\mathcal{A}_{\mu}{ }^{\rho}{ }_{\sigma}$ and $g_{\mu \nu}$ are independent there are 2 rather than 1 invariant that are linear in

$$
\mathcal{F}_{\mu \nu}{ }^{\rho}{ }_{\sigma} \equiv \partial_{\mu} \mathcal{A}_{\nu{ }_{\sigma}}{ }^{\rho}+\mathcal{A}_{\mu}{ }^{\rho} \mathcal{A}_{\nu}{ }^{\lambda}{ }_{\sigma}-(\mu \leftrightarrow \nu)
$$

1. The usual Ricci-like scalar $\mathcal{R} \equiv \mathcal{F}_{\mu \nu}{ }^{\mu \nu}$
2. The parity-odd Holst invariant $\mathcal{R}^{\prime} \equiv \epsilon^{\mu \nu \rho \sigma} \mathcal{F}_{\mu \nu \rho \sigma} / \sqrt{-g}$ [Hojman, Mukku, Sayed (1980); Nelson (1980); Holst (1995)]

In the GR case, where $\mathcal{A}_{\mu}{ }^{\rho}{ }_{\sigma}$ equals the Levi-Civita connection, $\mathcal{R}$ coincides with the Ricci scalar, $R$, but $\mathcal{R}^{\prime}$ vanishes. For this reason in metric-affine gravity $\mathcal{R}^{\prime}$ can be understood as a component of the connection

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The key idea here is to identify the inflaton with $\mathcal{R}^{\prime}$.
To do so $\mathcal{R}^{\prime}$ has to be a dynamical field, which is independent of the metric

## The minimal model

The simplest inflationary action that realizes this is

$$
S_{I}=\int d^{4} x \sqrt{-g}\left(\alpha \mathcal{R}+\beta \mathcal{R}^{\prime}+c \mathcal{R}^{\prime 2}\right)
$$

Indeed,

- for $c=0$ one can easily show, by solving the connection equations, that $S_{I}$ is equivalent to the Einstein-Hilbert action, having identified $\alpha=M_{P}^{2} / 2$
- for $c \neq 0$, standard auxiliary field methods show that an extra spin-0 parity odd dynamical field $\zeta^{\prime}$ (the "pseudoscalaron") is present and equals $\mathcal{R}^{\prime}$ on shell [Hecht, Nester, Zhytnikov (1996); Beltrán Jiménez, Maldonado Torralba (2019)]
- the $\beta \mathcal{R}^{\prime}$ term, a.k.a the Holst term, is also necessary to obtain a suitable inflaton potential, as we will see; the quantity $M_{P}^{2} /(4 \beta)$ is called the Barbero-Immirzi parameter [Immirzi (1996)]
$S_{I}$ can be recast in the following metric form (where the connection equals the Levi-Civita one)

$$
S_{I}=\int d^{4} x \sqrt{-g}\left[\frac{M_{P}^{2}}{2} R-\frac{(\partial \omega)^{2}}{2}-U\left(\zeta^{\prime}(\omega)\right)\right]
$$

where $U\left(\zeta^{\prime}\right)=c \zeta^{\prime 2}(c \geq 0$ for stability reasons $)$ and

$$
\zeta^{\prime}(\omega)=\frac{1}{2 c}\left(\frac{M_{P}^{2} \tanh X(\omega)}{4 \sqrt{1-\tanh ^{2} X(\omega)}}-\beta\right), \quad X(\omega) \equiv \sqrt{\frac{2}{3}} \frac{\omega}{M_{P}}+\tanh ^{-1}\left(\frac{4 \beta}{\sqrt{16 \beta^{2}+M_{P}^{4}}}\right)
$$

## Slow-roll inflation

The slow-roll approximation can be used when

$$
\epsilon \equiv \frac{M_{P}^{2}}{2}\left(\frac{1}{U} \frac{d U}{d \omega}\right)^{2} \ll 1, \quad \eta \equiv \frac{M_{P}^{2}}{U} \frac{d^{2} U}{d \omega^{2}} \ll 1
$$

and in this case the number of e-folds $N_{e}$ as a function of the field $\omega$ is given by

$$
N_{e}(\omega)=N(\omega)-N\left(\omega_{\mathrm{end}}\right), \quad N(\omega)=\frac{1}{M_{P}^{2}} \int^{\omega} d \omega^{\prime}\left(\frac{d U}{d \omega^{\prime}}\right)^{-1} U
$$

and $\omega_{\text {end }}$ satisfies $\epsilon\left(\omega_{\text {end }}\right)=1$. Then $n_{s}, r$ and $P_{R}$ (at horizon exit) are

$$
n_{s}=1-6 \epsilon+2 \eta, \quad r=16 \epsilon, \quad P_{R}=\frac{U / \epsilon}{24 \pi^{2} M_{P}^{4}}
$$

## Analytical formulæ for inflationary observables

$$
\begin{aligned}
\epsilon(\omega)= & \frac{4 M_{P}^{4} \cosh ^{2} X(\omega)}{3\left(M_{P}^{2} \sinh X(\omega)-4 \beta\right)^{2}}, \\
\eta(\omega)= & \frac{4 M_{P}^{2}\left(M_{P}^{2} \cosh (2 X(\omega))-4 \beta \sinh X(\omega)\right)}{3\left(M_{P}^{2} \sinh X(\omega)-4 \beta\right)^{2}}, \\
N(\omega)= & \frac{3}{4} \log (\cosh X(\omega))-\frac{3 \beta \arctan (\sinh X(\omega))}{M_{P}^{2}}, \\
n_{s}(\omega)= & 1-\frac{8 M_{P}^{4} \cosh ^{2} X(\omega)}{\left(M_{P}^{2} \sinh X(\omega)-4 \beta\right)^{2}} \\
& +\frac{8 M_{P}^{2}\left(M_{P}^{2} \cosh (2 X(\omega))-4 \beta \sinh X(\omega)\right)}{3\left(M_{P}^{2} \sinh X(\omega)-4 \beta\right)^{2}}, \\
r(\omega)= & \frac{64 M_{P}^{4} \cosh ^{2} X(\omega)}{3\left(M_{P}^{2} \sinh X(\omega)-4 \beta\right)^{2}}, \\
P_{R}(\omega)= & \frac{\left(\beta-\frac{M_{P}^{2} \sinh X(\omega)}{4}\right)^{2}\left(M_{P}^{2} \sinh X(\omega)-4 \beta\right)^{2} \operatorname{sech}^{2} X(\omega)}{128 \pi^{2} c M_{P}^{8}} .
\end{aligned}
$$

Moreover, the analytic expressions of $\omega_{ \pm}$(the two solutions of $\epsilon\left(\omega_{\text {end }}\right)=1$ ) are

$$
\omega_{ \pm}=\sqrt{\frac{3}{2}} M_{P}\left(\sinh ^{-1}\left( \pm \sqrt{\frac{192 \beta^{2}}{M_{P}^{4}}-4}-\frac{12 \beta}{M_{P}^{2}}\right)\right.
$$

## The pseudoscalaron mass and full potential




Left plot: the pseudoscalaron mass $m_{\zeta^{\prime}}$ and the corresponding value of $c$ that gives the observed $P_{R}$ at $N_{e}$ e-folds before the end of inflation
Right plot: the corresponding pseudoscalaron potential for $\beta=-80 M_{P}^{2}$

In the $\omega$ potential there is a plateau, which is larger the larger $|\beta|$ is and disappears when $\beta=0$. This is the reason why the $\beta \mathcal{R}^{\prime}$ term in $S_{I}$ is necessary

Given the shape of $U\left(\zeta^{\prime}(\omega)\right)$, we take $\omega_{\text {end }}$ such that $\left|\omega_{\text {end }}\right|=\min \left(\left|\omega_{+}\right|,\left|\omega_{-}\right|\right)$.

## Predictions for $n_{s}$ and $r$


$n_{s}$ and $r$ as functions of the canonically normalized pseudoscalaron $\omega$. In the inset the slow-roll parameters are given. This plot shows that viable slow-roll inflation with an appropriate $N_{e}$ occurs for $\omega$ slightly above the Planck scale. As an example we have set $\beta=-300 M_{P}^{2}$.

## Predictions for $n_{s}$ and $r$




Upper plots: $n_{s}$ and $r$ compared with the observational data. The green dots are the predictions of Starobinsky inflation.
Down plot: slow-roll parameters.
These plots show that slow-roll inflation not only occurs, but is also remarkably compatible with the most recent CMB observations provided by Planck and BK18 for large $|\beta|$ (i.e. small values of the Barbero-Immirzi parameter) and for an appropriate number of e-folds $N_{e}$

## Reheating: generalities

If $\omega$ decays into some SM particles with width $\Gamma_{\omega}$ the reheating temperature $T_{\mathrm{RH}}$ is

$$
T_{\mathrm{RH}} \gtrsim \min \left(\left(\frac{45 \Gamma_{\omega}^{2} M_{P}^{2}}{4 \pi^{3} g_{*}}\right)^{1 / 4},\left(\frac{30 \rho_{\mathrm{vac}}}{\pi^{2} g_{*}}\right)^{1 / 4}\right)
$$

where $g_{*}$ is the effective number of relativistic species in thermal equilibrium at temperature $T_{\mathrm{RH}}$ and $\rho_{\mathrm{vac}}$ is the vacuum energy density due to $\omega$

## Reheating: $\omega \rightarrow$ fermion pair

Let us first consider a fermion $f$ represented by a Dirac spinor $\Psi$ with action

$$
S_{f}=\int \sqrt{-g} \frac{1}{2} \bar{\Psi}\left(i \not \subset-m_{f}\right) \Psi+\text { h.c. }
$$

By using the connection equations one finds the following effective pseudoscalaron-fermion-fermion interaction

$$
\mathscr{L}_{\omega f f}=\frac{c_{\omega f f}}{M_{P}} \partial_{\mu} \omega \bar{\Psi} \gamma_{5} \gamma^{\mu} \Psi
$$

where

$$
c_{\omega f f}=\left[\frac{3 M_{P}}{1+16 B^{2}} \frac{d B}{d \omega}\right]_{\omega=0}=\sqrt{\frac{3 M_{P}^{4}}{8\left(M_{P}^{4}+16 \beta^{2}\right)}}, \quad B(\omega)=\left(\beta+2 c \zeta^{\prime}(\omega)\right) / M_{P}^{2}
$$

This effective interaction leads to the decay $\omega \rightarrow f f$ with width

$$
\Gamma_{\omega \rightarrow f f}=\left|c_{\omega f f}\right|^{2} \frac{m_{\omega} m_{f}^{2}}{2 \pi M_{P}^{2}} \sqrt{1-\frac{4 m_{f}^{2}}{m_{\omega}^{2}}}
$$

This can efficiently reheat the universe up to a temperature above the electroweak scale if $m_{f}$ is very large compared to that scale.
Such a fermion is not present in the SM, but it is possible to engineer a model where there is a very heavy fermion with sizable couplings to SM particles

## Reheating: $\omega \rightarrow$ scalar pair (e.g. a pair of Higgs bosons)

In order to keep our analysis as model independent as possible, we consider another channel: the decay of $\omega$ into two identical real scalar particles, e.g. two Higgs bosons. This is possible when there is a non-minimal coupling between the real (canonically normalized) scalar field $\phi$ in question and $\mathcal{R}$ in the action:

$$
S_{\mathrm{nm}}=\int \sqrt{-g} \frac{\xi \phi^{2}}{2} \mathcal{R}
$$

$S_{\mathrm{nm}}$ is known to be generated by quantum corrections (it is more natural to include it) Solving the connection equations one finds

$$
\mathscr{L}_{\omega \phi \phi}=\frac{c_{\omega \phi \phi}}{M_{P}} \partial_{\mu} \omega \phi \partial^{\mu} \phi \quad \text { where } \quad c_{\omega \phi \phi}=\left[\frac{48 \xi M_{P} B}{1+16 B^{2}} \frac{d B}{d \omega}\right]_{\omega=0}=\frac{4 \sqrt{6} \beta \xi}{\sqrt{M_{P}^{4}+16 \beta^{2}}}
$$

$\mathscr{L}_{\omega \phi \phi}$ only arises through the Holst term because $c_{\omega \phi \phi} \rightarrow 0$ as $\beta \rightarrow 0$ and gives

$$
\Gamma_{\omega \rightarrow \phi \phi}=\left|c_{\omega \phi \phi}\right|^{2} \frac{m_{\omega}^{3}}{16 \pi M_{P}^{2}} \sqrt{1-\frac{4 m_{\phi}^{2}}{m_{\omega}^{2}}}
$$

where $m_{\phi}$ is the mass of $\phi$. The channel $\omega \rightarrow \phi \phi$ can efficiently and naturally reheat the universe up to a temperature much above the electroweak scale, even if one identifies $\phi$ with the Higgs, so per se it does not require any beyond-the-SM physics. E.g. taking $m_{\phi} \ll m_{\omega}, g_{*} \sim 10^{2}$ and $\beta \gtrsim M_{P}^{2}$ one finds $T_{\mathrm{RH}} \gtrsim 10^{9}|\xi| \mathrm{GeV}$.

## Emergence of the equivalence principle

For any fixed spacetime point $X$, it is possible to choose a reference frame (called locally inertial frame) where the laws of physics are those without gravity in a small enough neighbourhood of $X$.

It is particularly interesting to see whether the equivalence principle holds in metric-affine theories as these are gravitational theories constructed starting from the geometrical principle of general covariance. Indeed, normally general covariance is seen as a consequence of the equivalence principle, but can one reverse this logic?

- We define the "physics without gravity" as some theory with ordinary matter, such as the one present in the SM and its common extensions. This can feature (pseudo)scalars, gauge fields and fermions, which are enough to account for all matter we observe and address the evidence of beyond-the-SM physics.
- Starting from the the general relativity principle the dynamical components of the distorsion that can be massless are only spin-1 and spin-0 fields for realistic theories (that must be stable and feature fermions and whose connection is, therefore, metric compatible). This was obtained using the results of [Neville (1978), (1981)] appropriately generalized to include matter fields.
- Therefore, at low enough energies the equivalence principle emerges: there are no fields of spin higher than 1 besides the graviton.


## Conclusions

- We have found the form of the action of a general metric-affine effective field theory with a non-dynamical distorsion
- It has been found that a pseudoscalar component of a dynamical connection, which is independent of the metric, can drive inflation in agreement with current data. This pseudoscalaron is identified with the parity odd Holst invariant and inflationary predictions in excellent agreement with data have been found for small values of the Barbero-Immirzi parameter, where the inflaton potential develops a plateau. The predictions approach, but do not quite reach, those of Starobinsky inflation as the Barbero-Immirzi parameter goes to zero; for finite values, on the other hand, the predictions significantly differ. Pseudoscalaron inflation can be tested by future CMB observations, such as those of LiteBIRD.
- Moreover, the decays of the pseudoscalaron into Higgs particles can efficiently reheat the universe after inflation up to a high enough temperature. This temperature could be further increased by other channels, such as decays into very massive fermions
- In a realistic metric-affine theory the equivalence principle always emerges at low enough energies


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## Thank you very much for your attention!

